

Logic design (2016 spring)

Quiz # 1

Name: _____ ID: _____

1. (30%+15%) Convert 455.1_9 to hexadecimal and then to binary.

Ans:

$$455.1_9 = 4 \times 9^2 + 5 \times 9^1 + 5 \times 9^0 + 1 \times 9^{-1} = 4 \times 81 + 5 \times 9 + 5 + 1/9 = 374 \frac{1}{9}_{10}$$

$$\frac{374}{16} = 23 \dots 6$$

$$\frac{23}{16} = 1 \dots 7$$

$$\frac{1}{16} = 0 \dots 1$$

$$1/9 \times 16 = 1 \frac{7}{9}$$

$$7/9 \times 16 = 12 \frac{4}{9}$$

$$4/9 \times 16 = 7 \frac{1}{9}$$

$$455.1_9 = 176.\underline{1C7}_{16} = 1\ 0111\ 0110.\underline{0001\ 1100\ 0111}_2 = 1\ 0111\ 0110.\underline{000111}_2$$

2. (40%) Subtract each of the following pairs of 5-bit 1's complement numbers by adding the complement of the subtrahend to the minuend and indicate when an overflow occurs.

(a) (20%) $10101 - 01001$

(b) (20%) $01101 - 11101$

(a)

$$\begin{array}{r} 10101 \\ + \underline{10110} \\ (1)01011 \end{array}$$

$$\begin{array}{r} \underline{1} \\ 01100 \end{array}$$

Overflow

(b)

$$\begin{array}{r} 01101 \\ + \underline{00010} \\ 01111 \end{array}$$

3. (15%) What number does 11010111 represent in a 6-2-2-1 weighted code for decimal digits?

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