

Logic design (2016 spring)

Quiz # 3

Name: _____ ID: _____

1. (50%) Eliminate the exclusive OR, and then factor to obtain a minimum product of sums

$$M'(K \oplus N') + MN + K'N$$

$$M'(K \oplus N') + MN + K'N$$

$$= M'(K'N' + KN) + MN + K'N$$

$$= K'M'N' + KM'N + MN + K'N$$

$$= K'M'N' + N(M + KM' + K')$$

$$= K'M'N' + N(M + K' + M')$$

$$= K'M'N' + N$$

$$= N + K'M'$$

$$= (K' + N)(M' + N)$$

2. (50%) Determine the following equation is always valid or not with algebraic proof

$$a'b + b'c + c'a = ab' + bc' + ca'$$

$$a'b + b'c + c'a$$

$$= a'b(c+c') + (a+a')b'c + (b+b')ac'$$

$$= a'bc + a'bc' + ab'c + a'b'c + abc' + ab'c'$$

$$= (a'bc + a'b'c) + (a'bc' + abc') + (ab'c + ab'c')$$

$$= a'c + bc' + ab'$$