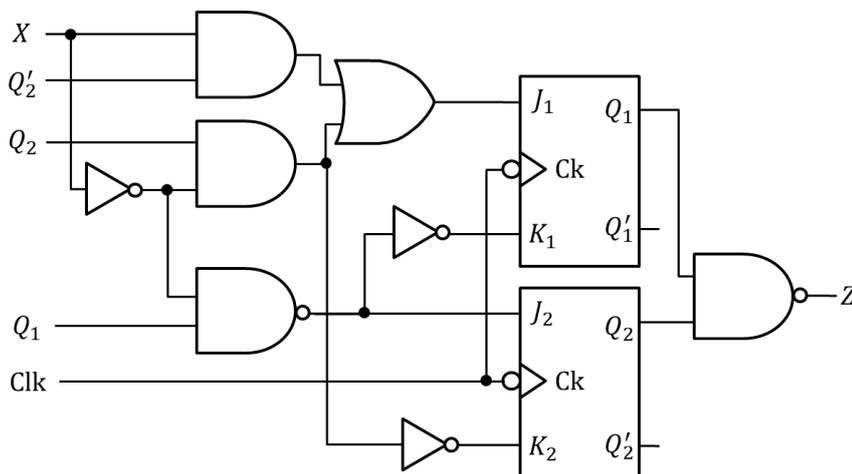


Logic design (2017 fall)

Quiz # 13

Name: \_\_\_\_\_ ID: \_\_\_\_\_

1. (100%) Consider the circuit shown below.
  - (a) (20%) Derive the flip-flop input equations ( $J_1, K_1, J_2, K_2$ ). Note that each equation needs to be expressed in the minimum SOP form.
  - (b) (25%) Derive the next-state equation for each FF from its input equations and derive the equation for output  $Z$ . Note that each equation needs to be expressed in the minimum SOP form.
  - (c) (30%) Complete the transition table for the circuit.
  - (d) (15%) Construct the state graph for the circuit using the given state assignment.
  - (e) (5%) Does the circuit have any unused states?
  - (f) (5%) Is the circuit a Mealy or Moore machine?



Transition table

Present State $Q_1 Q_2$	Next State $Q_1^+ Q_2^+$		$Z$
	$X = 0$	$X = 1$	
00	01	11	1
01	11	00	1
11	01	10	0
10	00	11	1

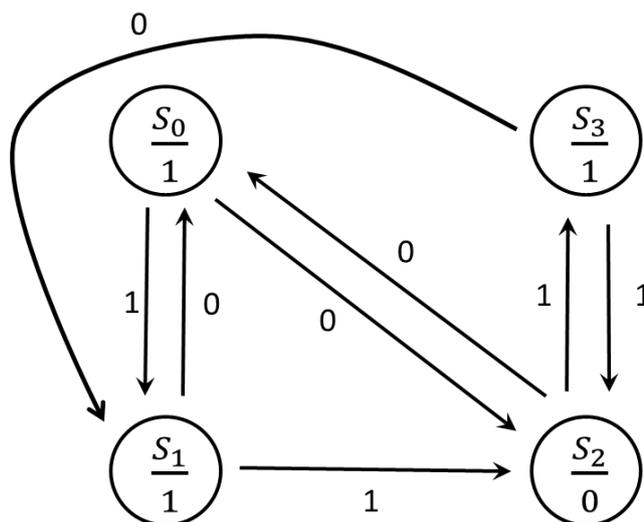
Ans:

(a)  $J_1 = XQ_2' + X'Q_2$      $K_1 = X'Q_1$   
 $J_2 = X + Q_1'$      $K_2 = X + Q_2'$

(b)  $Q_1^+ = J_1Q_1' + K_1'Q_1$   
 $= (XQ_2' + X'Q_2)Q_1' + (X'Q_1)'Q_1$   
 $= XQ_1'Q_2' + X'Q_1'Q_2 + XQ_1 = XQ_1 + XQ_2' + X'Q_1'Q_2$   
 $Q_2^+ = J_2Q_2' + K_2'Q_2$   
 $= (X + Q_1')Q_2' + (X + Q_2')'Q_2$   
 $= XQ_2' + Q_1'Q_2' + X'Q_2$   
 $Z = (Q_1Q_2)' = Q_1' + Q_2'$

State assignment

$S_0$	01
$S_1$	00
$S_2$	11
$S_3$	10



(e) No

(f) The circuit is a Moore machine .