

Logic design (Fall 2021)

Quiz # 12

Name: _____ ID: _____

1. (100%) Design a 3-bit counter in the sequence: (C, B, A) = 111, 101, 011, 110, 000, 010, (repeat) 111, / 111, 100, 101, 001, 000, 110, (repeat) 111, with D flip-flops and J-K flip-flops. Note that you just need to drive the Boolean equations for the input of each flip-flops.

(a). (28%) Complete the following table.

(b). (36%) Use D flip-flops.

$$C^+ =$$

$$B^+ =$$

$$A^+ =$$

(c). (36%) Use J-K flip-flops.

$$J_C =$$

$$K_C =$$

$$J_B =$$

$$K_B =$$

$$J_A =$$

$$K_A =$$

Ans:

(a).

C	B	A	$C^+B^+A^+$	J_C	K_C	J_B	K_B	J_A	K_A
0	0	0	010	0	X	1	X	0	X
0	0	1	XXX	X	X	X	X	X	X
0	1	0	111	1	X	X	0	1	X
0	1	1	110	1	X	X	0	X	1
1	0	0	XXX	X	X	X	X	X	X
1	0	1	011	X	1	1	X	X	0
1	1	0	000	X	1	X	1	0	X
1	1	1	101	X	0	X	1	X	0

(b).

	C	0	1
BA			
00		0	X
01		X	0
11		1	1
10		1	0
		C^+	

	C	0	1
BA			
00		1	X
01		X	1
11		1	0
10		1	0
		B^+	

	C	0	1
BA			
00		0	X
01		X	1
11		0	1
10		1	0
		A^+	

$$C^+ = AB + BC'$$

$$B^+ = B' + C'$$

$$A^+ = AC + A'BC'$$

(c).

	C	0	1
BA			
00		0	X
01		X	X
11		1	X
10		1	X

J_C

	C	0	1
BA			
00		X	X
01		X	1
11		X	0
10		X	1

K_C

	C	0	1
BA			
00		1	X
01		X	1
11		X	X
10		X	X

J_B

	C	0	1
BA			
00		X	X
01		X	X
11		0	1
10		0	1

K_B

	C	0	1
BA			
00		0	X
01		X	X
11		X	X
10		1	0

J_A

	C	0	1
BA			
00		X	X
01		X	0
11		1	0
10		X	X

K_A

$$J_C = B$$

$$K_C = A' + B'$$

$$J_B = 1$$

$$K_B = C$$

$$J_A = BC'$$

$$K_A = C'$$

Ans:

(a).

C	B	A	$C^+B^+A^+$	J_C	K_C	J_B	K_B	J_A	K_A
0	0	0	110	1	X	1	X	0	X
0	0	1	000	0	X	0	X	X	1
0	1	0	XXX	X	X	X	X	X	X
0	1	1	XXX	X	X	X	X	X	X
1	0	0	101	X	0	0	X	1	X
1	0	1	001	X	1	0	X	X	0
1	1	0	111	X	0	X	0	1	X
1	1	1	100	X	0	X	1	X	1

(b).

BA \ C	0	1
00	1	1
01	0	0
11	X	1
10	X	1

C^+

BA \ C	0	1
00	1	0
01	0	0
11	X	0
10	X	1

B^+

BA \ C	0	1
00	0	1
01	0	1
11	X	0
10	X	1

A^+

$$C^+ = A' + B$$

$$B^+ = A'B + A'C'$$

$$A^+ = A'C + B'C \text{ or } A'B + B'C$$

(c).

	C	0	1
BA			
00		1	X
01		0	X
11		X	X
10		X	X

J_C

	C	0	1
BA			
00		X	0
01		X	1
11		X	0
10		X	0

K_C

	C	0	1
BA			
00		1	0
01		0	0
11		X	X
10		X	X

J_B

	C	0	1
BA			
00		X	X
01		X	X
11		X	1
10		X	0

K_B

	C	0	1
BA			
00		0	1
01		X	X
11		X	X
10		X	1

J_A

	C	0	1
BA			
00		X	X
01		1	0
11		X	1
10		X	X

K_A

$J_C = A'$

$K_C = AB'$

$J_B = A'C'$

$K_B = A$

$J_A = C$

$K_A = B + C'$