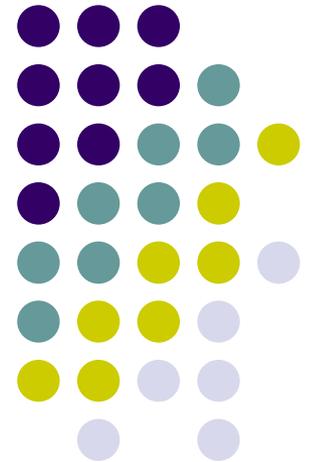


Chapter 2 Logic Simulation

電路邏輯模擬



Logic Simulation



- Purposes
 - Verification
 - Debugging
 - Studying design alternative (cost/speed)
 - Computing expected behavior for tests
- Simulation-based design verification
 - To check correct operations:
 - e.g. delays of critical paths
 - free of critical races & oscillation
 - Problem is that tests are hand crafted; Very hard to prove that a test is complete.
 - Formal and assertion-based verification required

Modeling for Circuit Simulation



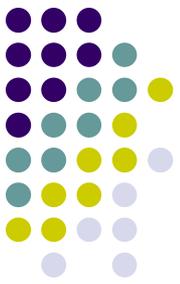
- Circuit models
 - Modeling levels
 - Behavioral, logic, switch, timing, circuit
 - Modeling description (languages)
- Signal models
 - Logic value models
 - Timing value models
- Choices of models determine the complexity and accuracy of simulation

Level of Circuit Modeling (1/2)



- Electronic system level
 - Software+hardware
 - Transaction/cycle-accurate functions
 - C/C++, SystemC, SystemVerilog, etc.
- Register-Transfer-Level (RTL)
 - Define bit and timing (almost) accurate architecture for sign-off
 - VHDL and Verilog
- Logic/cell/gate level
 - Interconnected Boolean gates
 - AND, OR, NOR, NAND, NOT, XOR, Flip-flops, Transmission gates, buses, etc.
 - Suitable for logic design, verification and test

Level of Circuit Modeling (2/2)



- Switch level
 - Interconnects of ideal transistor switch
 - Need transistor size, node R and C to determine logic value
 - Zero delay in timing
 - Suitable for full-custom high-performance ASIC
- Timing level
 - Use transistors with detailed device models
 - Calculate charge/discharge current with transistor's voltage-current model and obtain node voltage as a function of time
 - Mainly for post-PR timing verification, e.g., Timemill™
- Circuit level
 - Lowest level, ultimate in simulation accuracy
 - Obtain timing by solving the equations relating branch/loop current and node voltage
 - Critical timing analysis for digital circuits
 - Mixed-signal circuit simulation

Logic States for Simulation



- **Two states (0, 1) for combinational and sequential circuits with known initial states.**
- **Three states (0, 1, X) for sequential circuits with unknown initial states**
 - X (unknown state) for cases when the logic value cannot be determined
 - X can be either 0 or 1.
 - Sources: uninitialized FF, bus, memory, multi-cycle paths, etc.

Logic Operations with X



AND	0	1	x
0	0	0	0
1	0	1	x
x	0	x	x

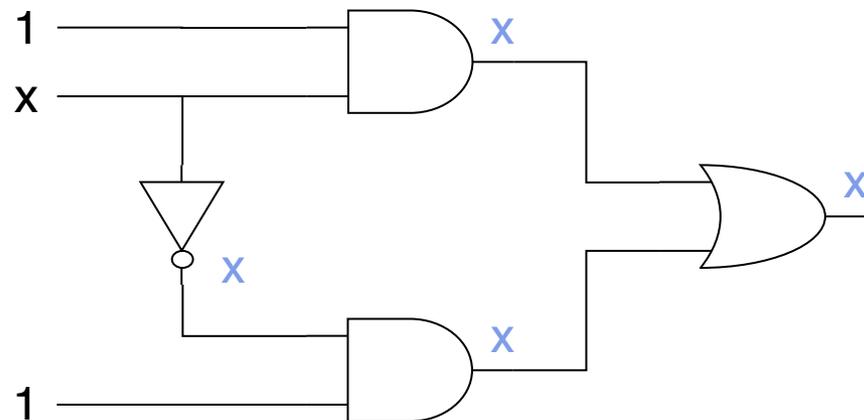
OR	0	1	x
0	0	1	x
1	1	1	1
x	x	1	x

Problems with 3-Valued Logic

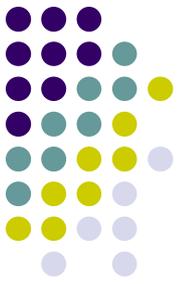


- May cause information loss
 - Fail determining the logic value even though that value can be easily determined
 - Example:

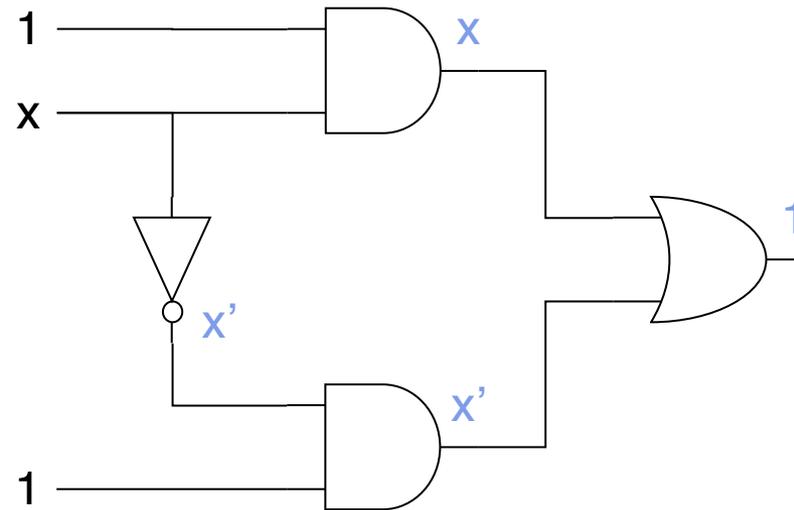
The output is evaluated as x even though it should be 1 regardless of the actual value of x



Symbolic Simulation of “x”



- Treat “x” as a signal
 - NOT $x = x'$
 - $x + x' = 1$



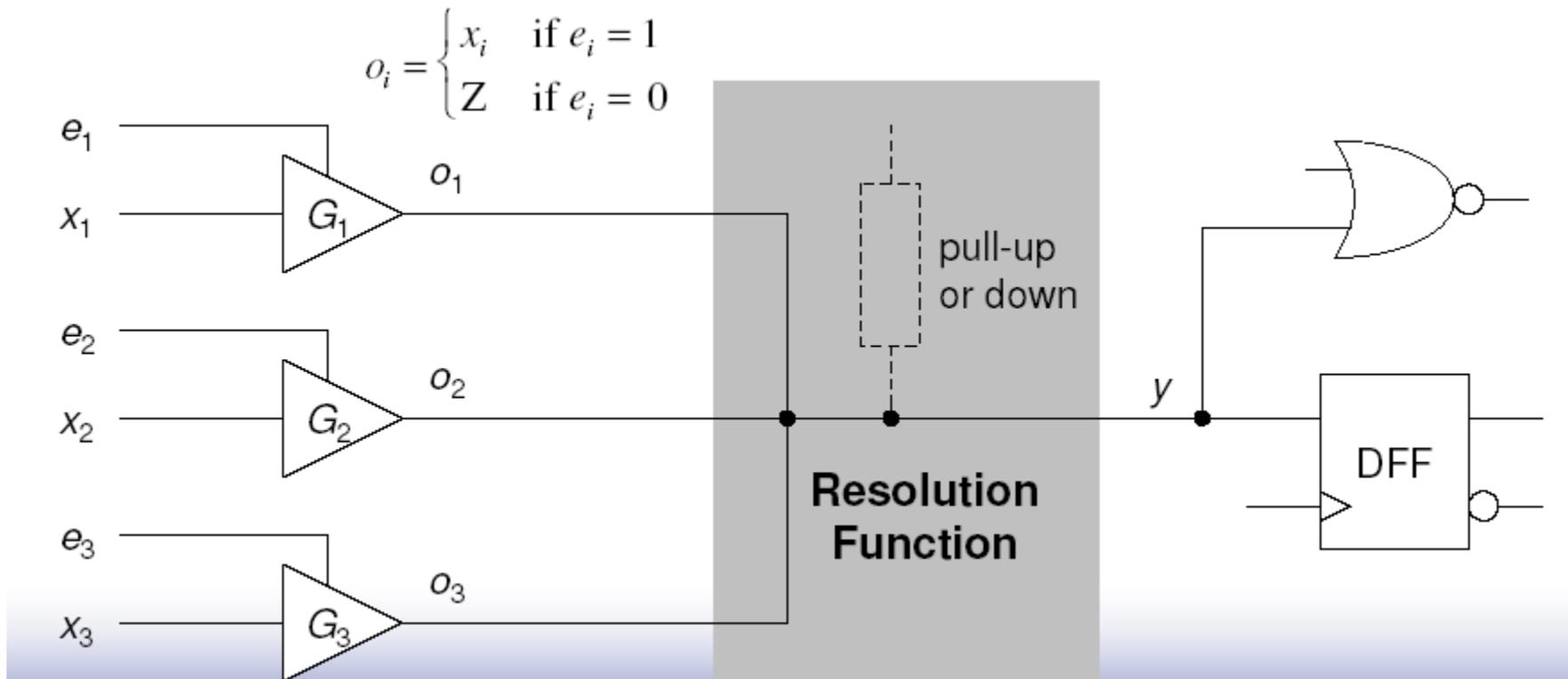
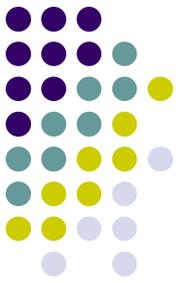
- Problem
 - There can be multiple sources of X, e.g., Flip-flops
 - One “x” for each unknown value (x_1, x_2, \dots)
 - Impractical for large circuits, e.g., $x_1 + x_2 = ?$

High-Impedance State Z



- Floating state: a node w/o a path conducting to either Vdd or Gnd
- Logic state of Z is interpreted dynamically
 - Single floating node
 - Same as its driven value before becoming floating
 - A set of floating nodes get connected
 - Depends on charge sharing, may become uncertain
 - A floating node connected to Vdd/Gnd becomes 1/0
 - When multiple source drive a floating node, the value depends on the strength of the driving logics.
- Most MOS circuits containing dynamic logic require four states (0, 1, x, z) for simulation

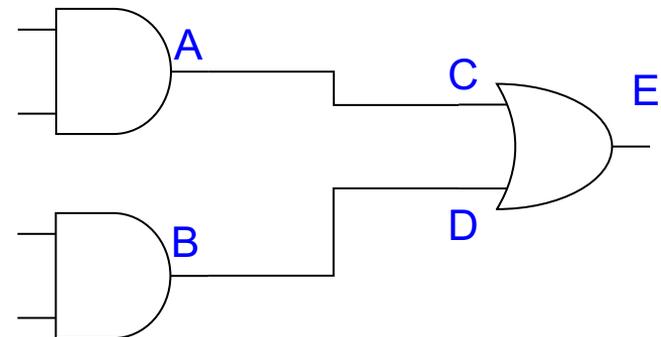
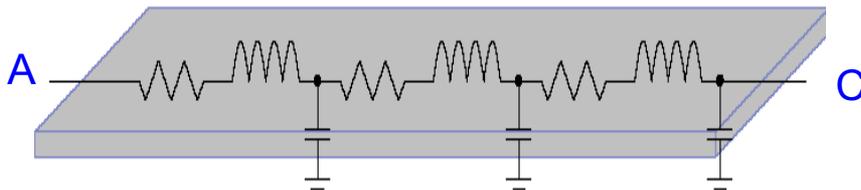
An Example of High-Z Bus



Delay (Timing) Models



- Delay of a logic element
 - Time between an input change (cause) and the output change (effect), e.g. C->E or D->E
 - Called gate delay, pin-pin delay, or switching delay
- Interconnect delay
 - Time between the generation of a signal transition at a gate output and its arrival at the input of a fanout gate, e.g. A->C, or B-> D
 - Or called switching delay
 - Consider R, C (L) effects

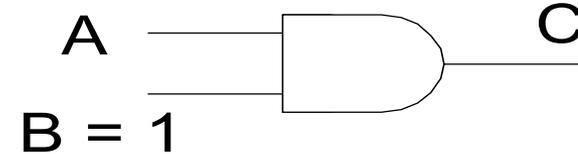
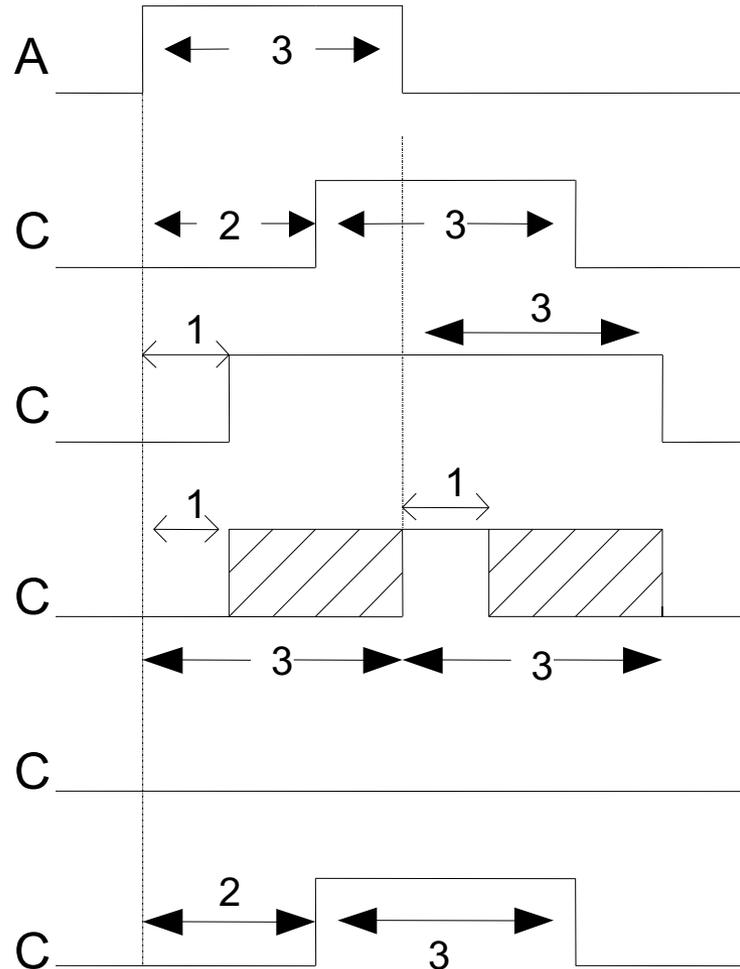


Terms for Cell Delay Models



- Zero and unit delay
- Rise (fall) delay
 - Gate delays of different final output states
- Inertia delay
 - Minimum pulse width to cause a transition
 - Used for filtering input/output pulse
 - Input inertia delay: minimum pulse width for input
 - Output inertia delay: minimum pulse width for output
- Min/Max Delay
 - The minimum or maximum bound of a gate delay
- Transition time
 - Time for a signal to transit from 0 to 1 or 1 to 0.

Delay Models Examples



transport delay = 2
(transition-independent)

rise delay = 1
fall delay = 3

min-max delay
(transition independent)
 $1 \leq d \leq 3$

input inertia delay = 4

input inertia delay = 2
& transport delay = 2

Common Cell Delay Models



- Table-based
 - A pin-pin min/max rise/fall delay of a cell = $f(CL, Tr)$
 - CL =output load
 - Tr =input transition time
- Current-source based
 - A voltage-controlled current source $I(V_i, V_o)$
 - I : V_{dd} to Gnd current
 - V_i : input voltage
 - V_o : output voltage
 - More accurate in terms of noise, but more CPU intensive
- Interconnect delays
 - Elmore delay

Modeling Levels and Signals



level	Circuit Description	Signal	Timing Resolution	Application
ESL	SystemC	0,1	transaction	system
Behavior	HDL	0,1	cycle	architecture
Logic	gate-level HDL	0, 1, X, Z (with signal strength)	zero, unit, multiple cell delays	logic design and test
Switch	transistor, RC interconnects	0, 1, X (with signal strength)	zero, possible gross-grain timing	full-custom logic verification
Timing	same as above (SPICE)	Analog	fine-grain time	timing verification
Circuit	same as above (SPICE)	Analog	continuous time	timing/analog verification

Types of Logic Simulators



- **Compiled-driven simulators**
 - The compiled code is generated from an RTL or gate-level description of the circuit
 - Simulation is simply execution of the compiled code
- **Event-driven Simulators**
 - Simulate only those signals with value changes
 - Only propagate necessary events (value changes)

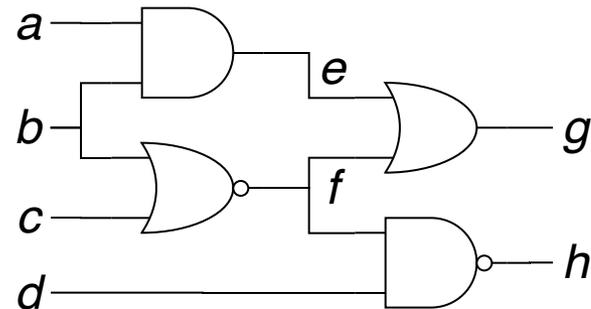
Compiled Simulation



- A circuit is simulated by executing a **compiled code** of the circuit.
- Levelization
 - to ensure that a signal is evaluated after all its sources are evaluated

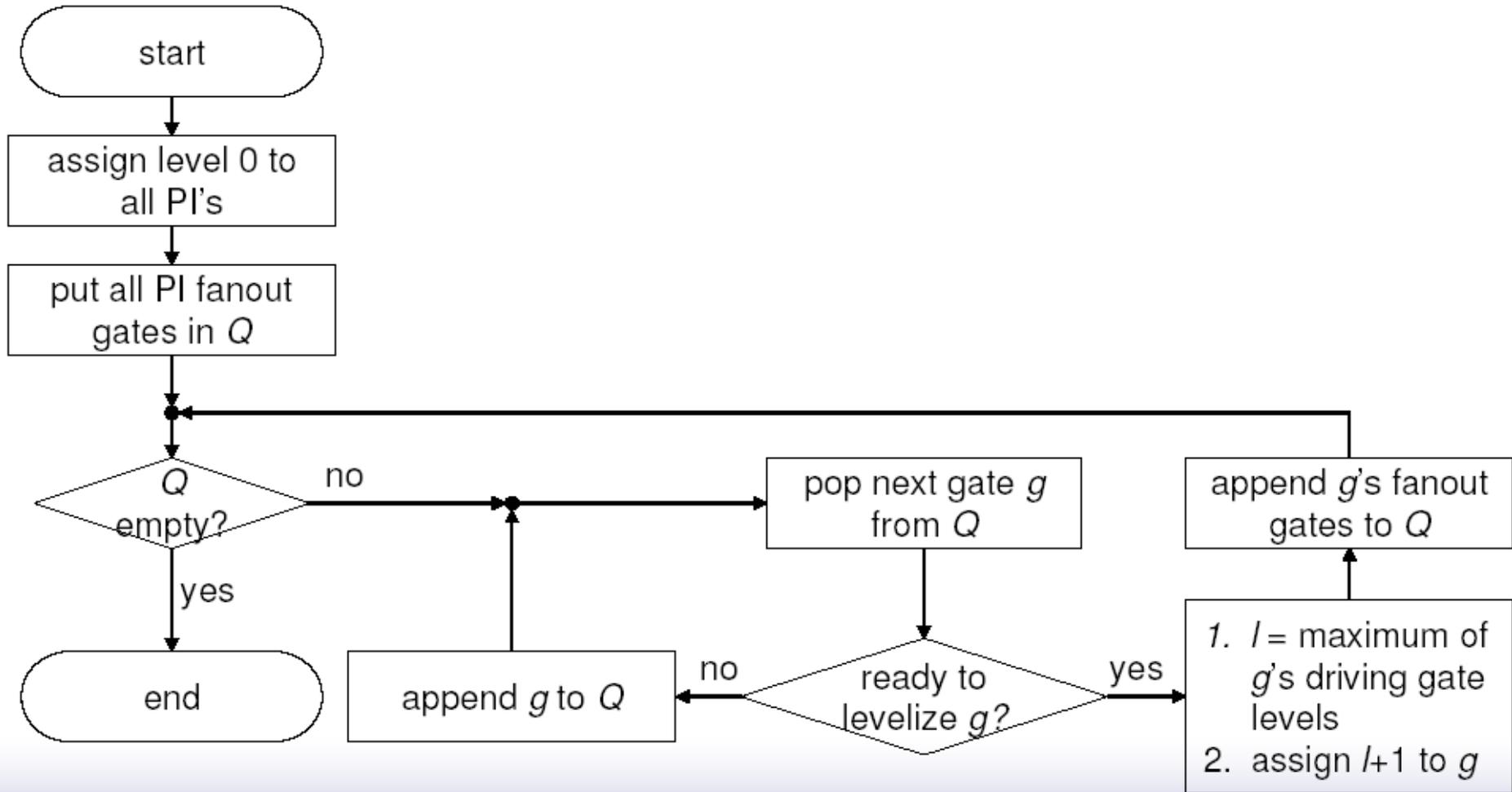
Levelization

- Assign all PI's level 0
- The level of gate G is
$$L_g = 1 + \max(L_1, L_2, \dots)$$
where L_i 's are G's input gates



- level 0: a, b, c, d
- level 1: e, f
- level 2: g, h

Flow of Levelization



Example of Levelization

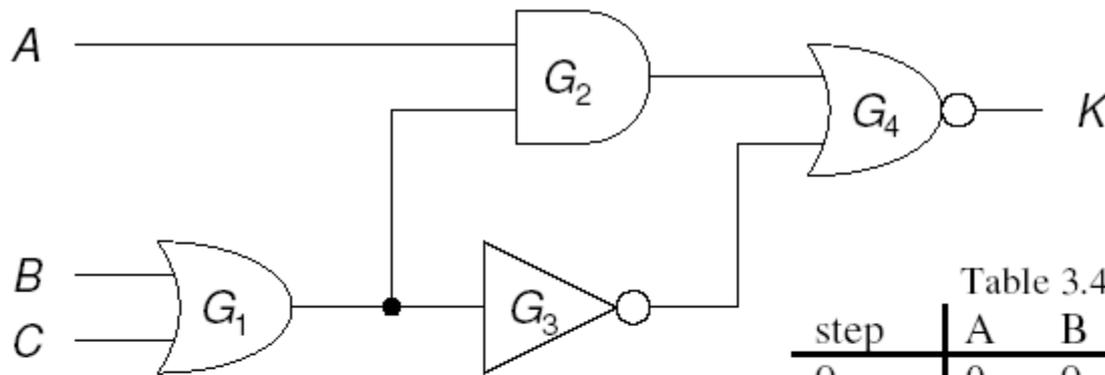
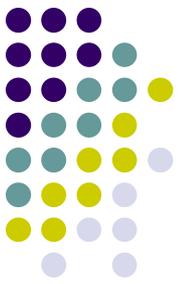


Table 3.4: The levelization process of circuit

step	A	B	C	G_1	G_2	G_3	G_4	Q
0	0	0	0					$\langle G_2, G_1 \rangle$
1	0	0	0					$\langle G_1, G_2 \rangle$
2	0	0	0	1				$\langle G_2, G_3 \rangle$
3	0	0	0	1	2			$\langle G_3, G_4 \rangle$
4	0	0	0	1	2	2		$\langle G_4 \rangle$
5	0	0	0	1	2	2	3	$\langle \rangle$

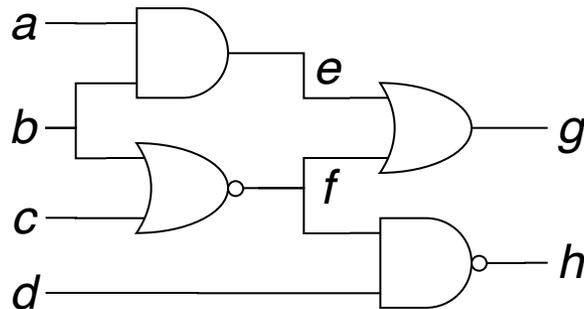
□ The following orders are produced

- $G_1 \Rightarrow G_2 \Rightarrow G_3 \Rightarrow G_4$
- $G_1 \Rightarrow G_3 \Rightarrow G_2 \Rightarrow G_4$

Compiled Simulation – cont'd



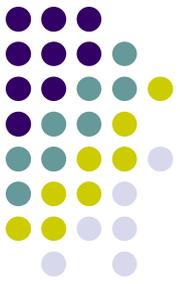
- Code generation & execution



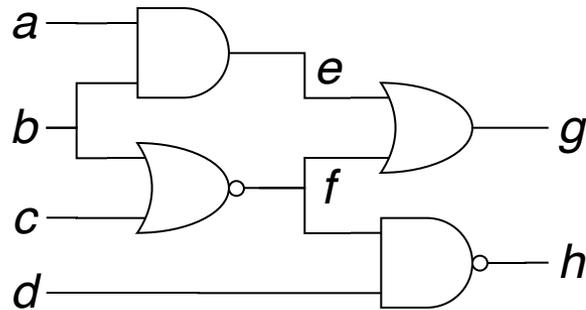
```
while (1) {  
    read_in(a,b,c,d);  
    e = AND(a,b);  
    f = NOR(b,c);  
    g = OR(e,f);  
    h = NAND(d,f);  
    print_out(g,h);  
}
```

- Very effective for 2-state (0,1) simulation
 - Can be compiled directly into machine codes
- Mainly for functional verification, where timing is irrelevant

Compiled Simulation – Example in C

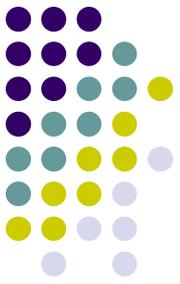


- Code generation in C



```
#include <stdlib.h>
int main(){
    unsigned int a=0xF; //1111
    unsigned int b=0xA; //1010
    unsigned int c=0x8; //1000
    unsigned int d=0x7; //0111
    unsigned int e, f, g, h;
    e = a&b;
    f = ~(b|c);
    g = e|f;
    h = ~(d&f);
    printf("g,h=%X,%X", g, h);
}
```

Problems with Compiled Simulation

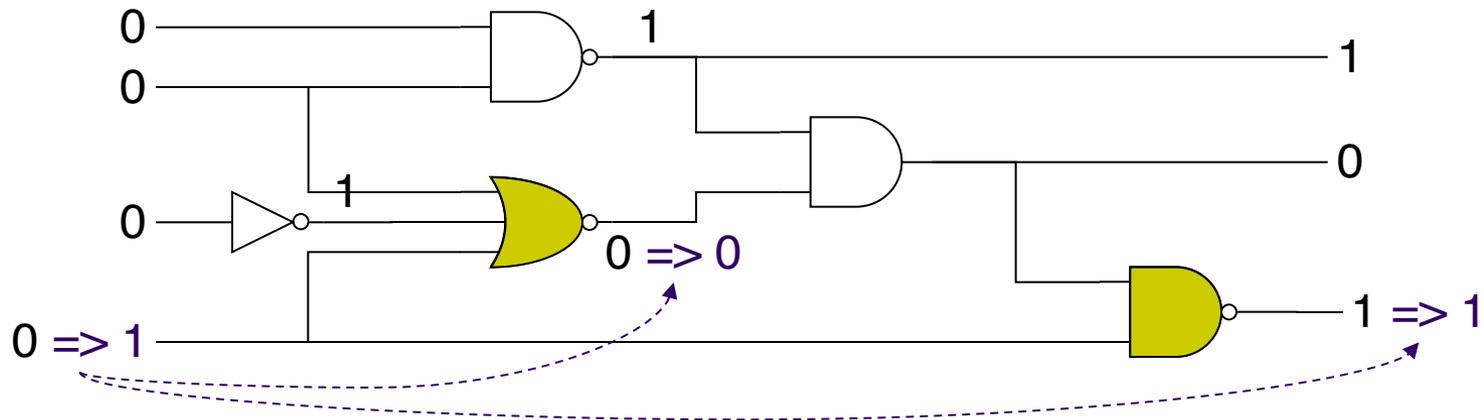


- Zero-delay model
 - Timing problems, e.g., glitches and races, cannot be modeled
- Simulation time could be long
 - Proportional to $\Omega(\text{input vectors} \times \text{number of gates})$
 - Entire circuit is evaluated even though typically only 1-10% of signals change at any time
 - Note RTL compiled simulation is different and fast, since branching can be used.

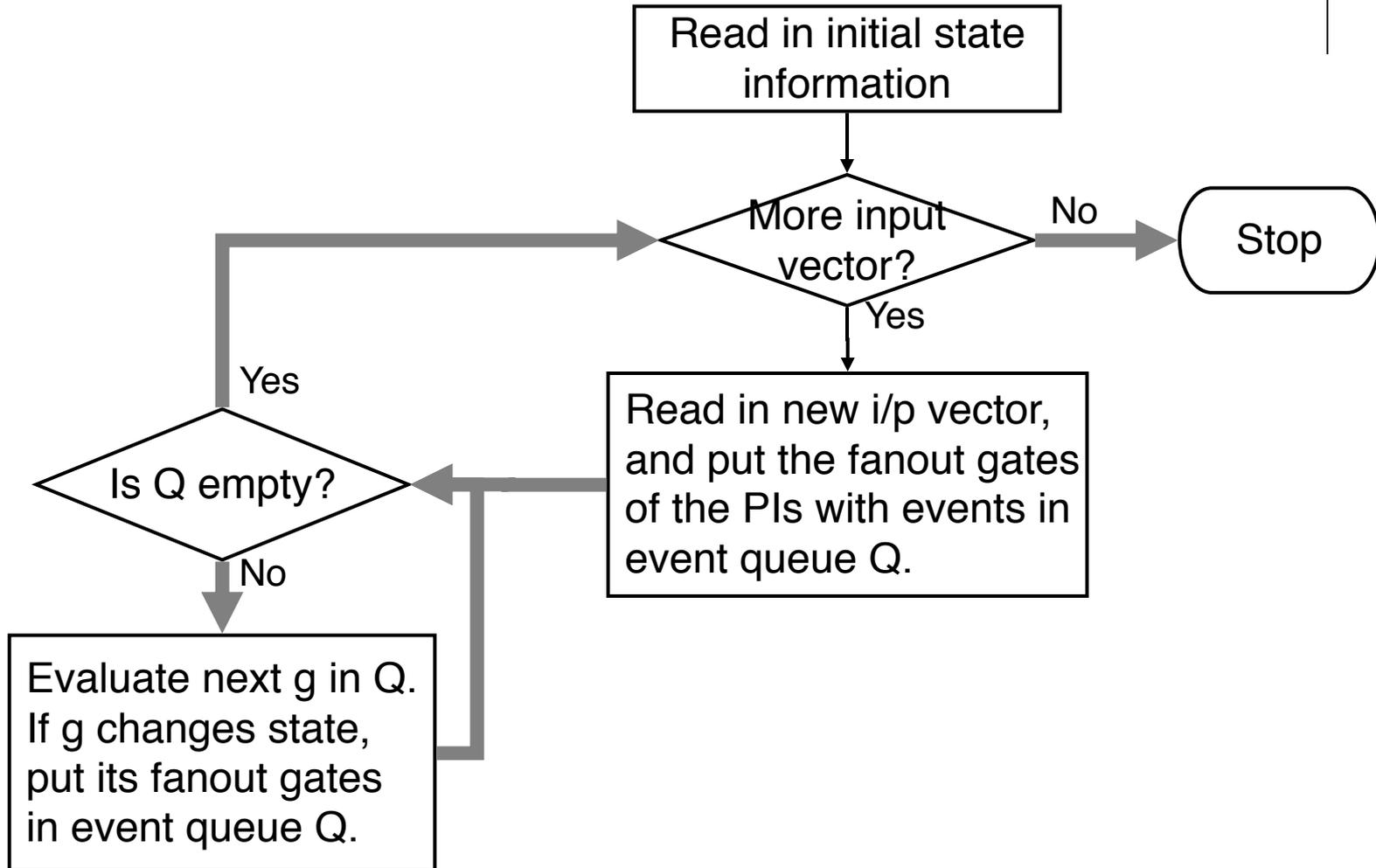
Event-Driven Simulation



- An event is a change in value of a signal line
- An event-driven simulator evaluates a gate (element) only if one or more events occur at its inputs
 - Only does the necessary amount of work
 - Follows the path of signal flow



Zero-Delay Event-Driven Simulation

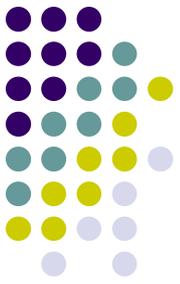


Gate Evaluation – Table Lookup



- The most straightforward and easy way to implement
 - For binary logic, 2^n entries for n -input logic element
 - May use the input value as table index
 - Table size increases exponentially with the number of inputs
- Could be inefficient for multi-valued logic
 - A k -symbol logic system requires a table of 2^{mn} entries for an n -input logic element
 - $m = \log_2 k$
 - Table indexed by mn -bit words

Gate Evaluation – Input Scanning



- Assume that only dealing w/ AND, OR, NAND, and NOR primitive gates
- These gates can be characterized by controlling value c and inversion i
 - The value of an input is said to be controlling if it determines the gate output value regardless of the values of other inputs

	c	i
AND	0	0
OR	1	0
NAND	0	1
NOR	1	1

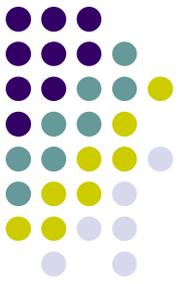
Input Scanning – cont'd



I/P of a 3-input primitive gate			O/P
c	x	x	$c \oplus i$
x	c	x	$c \oplus i$
x	x	c	$c \oplus i$
c'	c'	c'	$c' \oplus i$

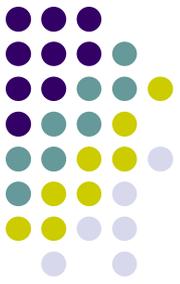
```
Evaluate(G,c,i) {  
    u_values = false;  
    for every input value v of G{  
        if (v == c) return c⊕i;  
        if (v == x) u_values = true;  
    }  
    if (u_values) return x;  
    return c'⊕i;  
}
```

Gate Evaluation – Input Counting



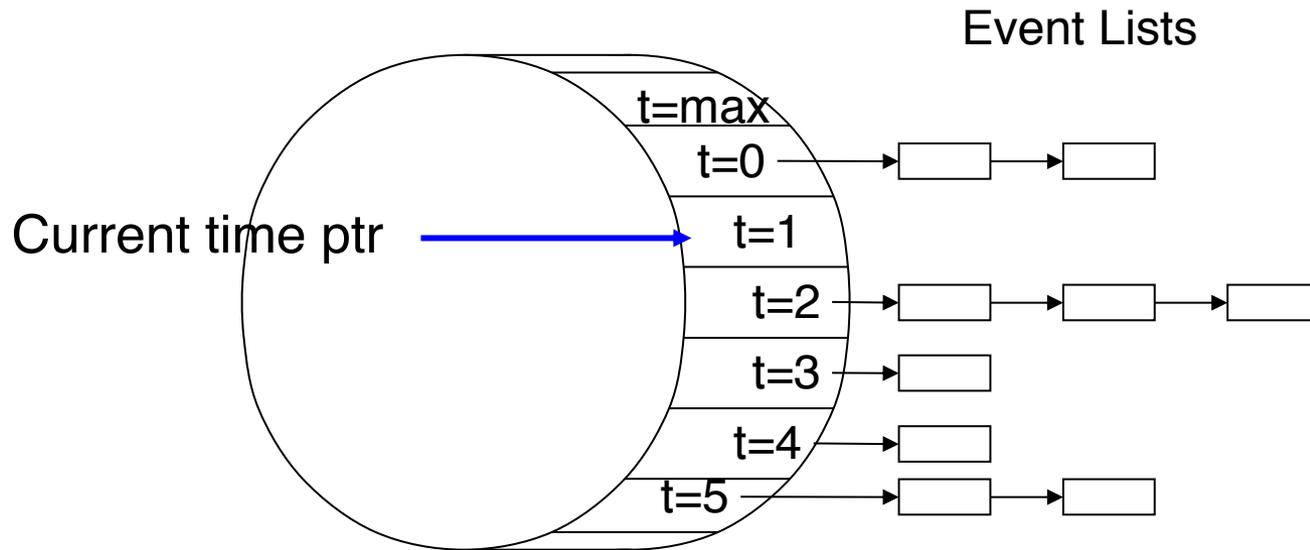
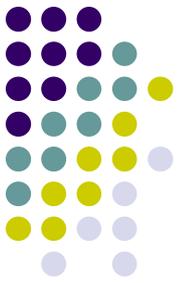
- To evaluate the output, it's sufficient to know
 - Whether any input equals c
 - If not, whether any input equals x
- Simply maintain c_count & x_count
 - Example: AND gate
 - $0 \Rightarrow 1$ at one input: $c_count--$
 - $0 \Rightarrow x$ at one input: $c_count--$, $x_count++$
- ```
Evaluate(G, c, i) {
 if (c_count > 0) return $c \oplus i$;
 if (x_count > 0) return x ;
 return $c' \oplus i$;
}
```

# Event-Driven Simulation with Delays



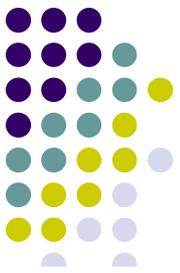
- While ( event list is not empty ){  
    t = next time in list;  
    process entries for time t;  
}
- The key is to construct a queue entry for every time point

# Time wheel

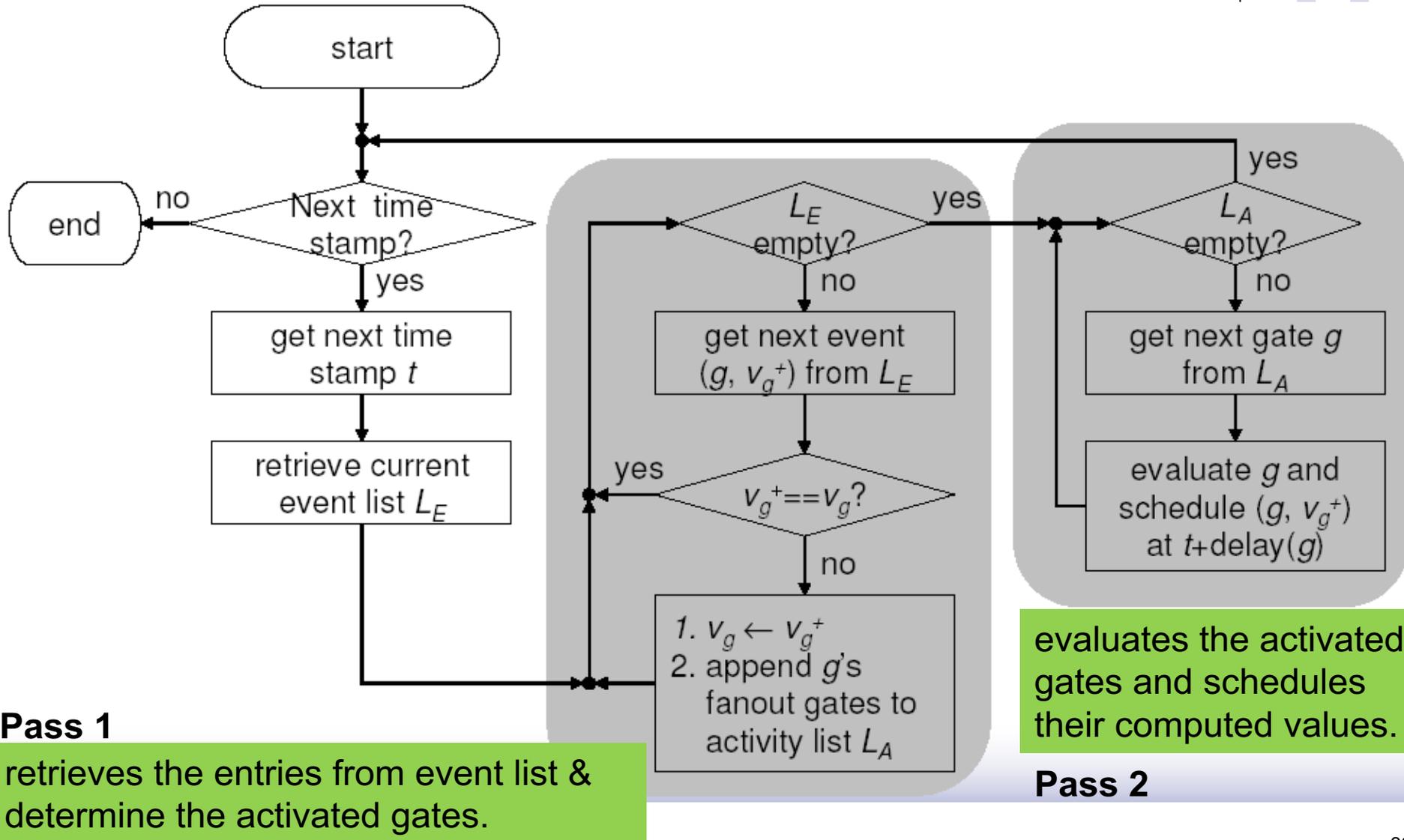


- Max units is the largest delay experienced by any event
  - All gates + interconnects
  - A total of  $\text{max}+1$  slots

# Flow of Simulation with Delays



## Algorithm 1 (two-pass)



# Simulation with Delays



## Algorithm 1

**Activated** =  $\phi$

For every event  $(g, v_g^+)$  at list of time  $t$  { //from  $L_E$   
if  $(v_g^+ \neq v_g)$  //  $v_g$  is the original value at signal  $g$  {

$v_g = v_g^+$ ;

for every  $j$  on fanout list of  $g$  {  
update input value of  $j$ ;

add  $j$  to  $L_A$  if  $j$  is not a member of  $L_A$ ;

} /\* for \*/

} /\* if \*/

} /\* for \*/

For every  $g \in L_A$  {

$v_g^+ = \text{evaluate}(g)$ ;

schedule  $(g, v_g^+)$  for time  $t + \text{delay}(g)$ ;

}

# Two-Pass Algorithm

## Example

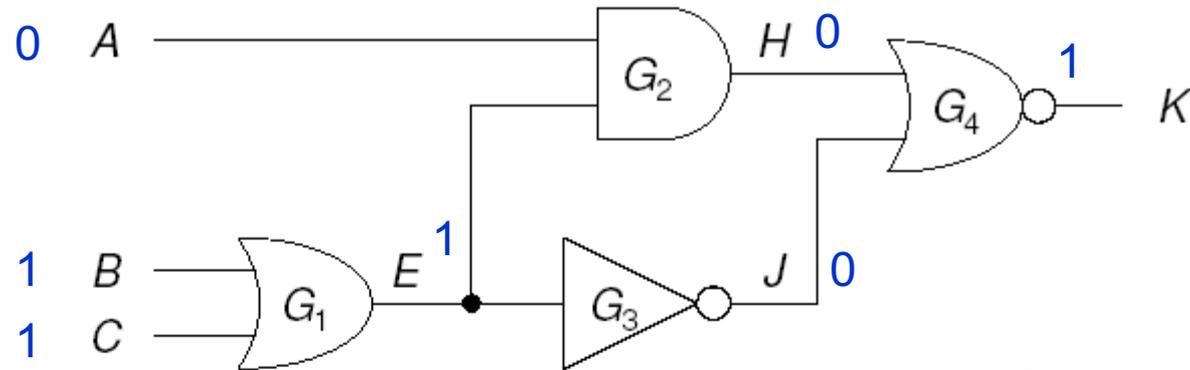


Table 3.5: Two-pass event-driven simulation

| Time | $L_E$             | $L_A$         | Scheduled events        |
|------|-------------------|---------------|-------------------------|
| 0    | $\{(A,1)\}$       | $\{G_2\}$     | $\{(H,1,8)\}$           |
| 2    | $\{(C,0)\}$       | $\{G_1\}$     | $\{(E,1,10)\}$          |
| 4    | $\{(B,0)\}$       | $\{G_1\}$     | $\{(E,0,12)\}$          |
| 8    | $\{(A,0),(H,1)\}$ | $\{G_2,G_4\}$ | $\{(H,0,16),(K,0,14)\}$ |
| 10   | $\{(E,1)\}$       |               |                         |
| 12   | $\{(E,0)\}$       | $\{G_2,G_3\}$ | $\{(H,0,20),(J,1,16)\}$ |
| 14   | $\{(K,0)\}$       |               |                         |
| 16   | $\{(H,0),(J,1)\}$ | $\{G_4\}$     | $\{(K,0,22)\}$          |
| 20   | $\{(H,0)\}$       |               |                         |
| 22   | $\{(K,0)\}$       |               |                         |

Gate delay

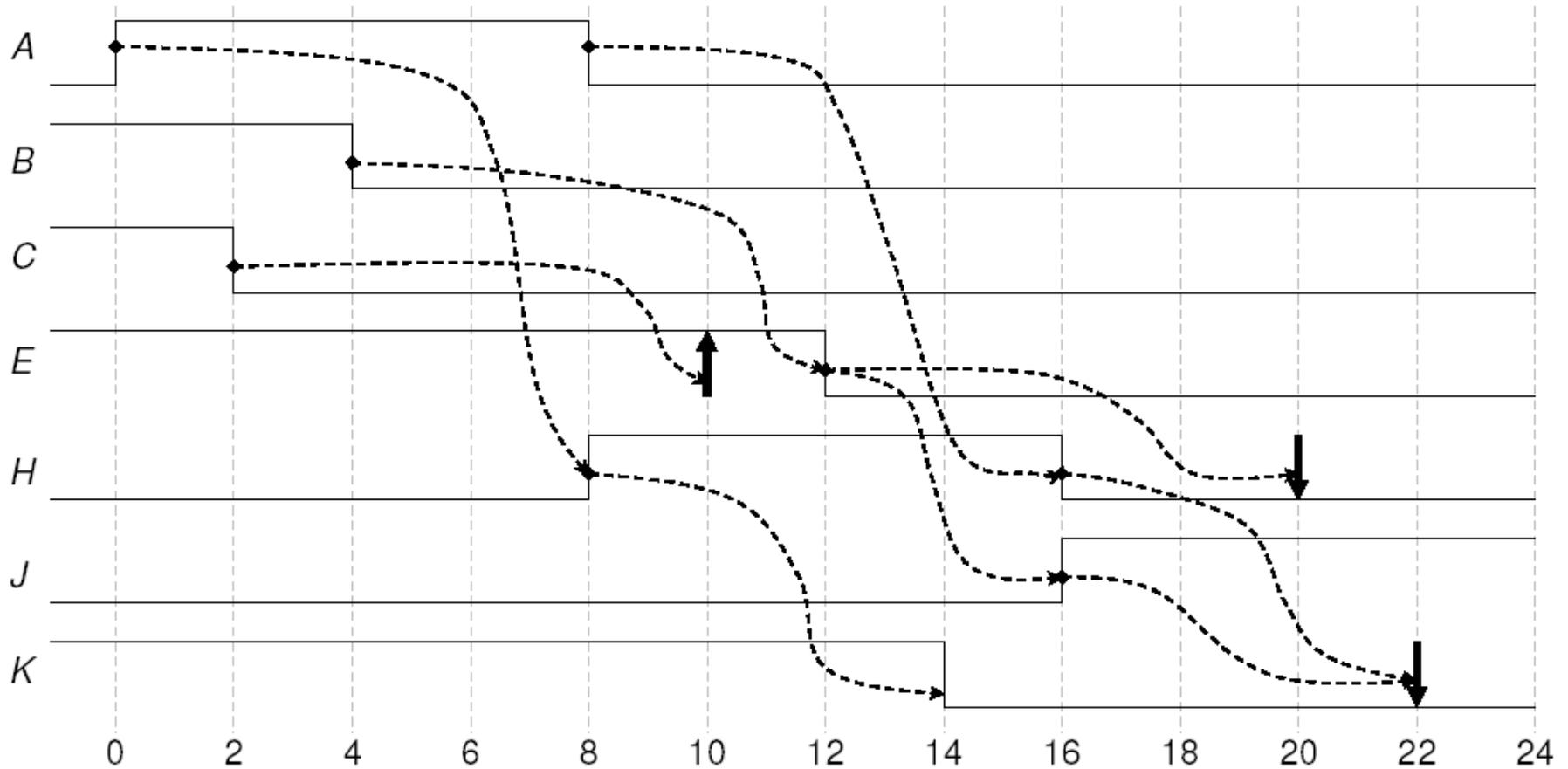
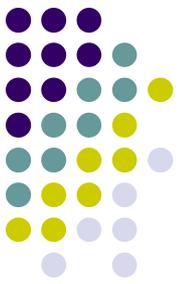
$G_1$ : 8ns

$G_2$ : 8ns

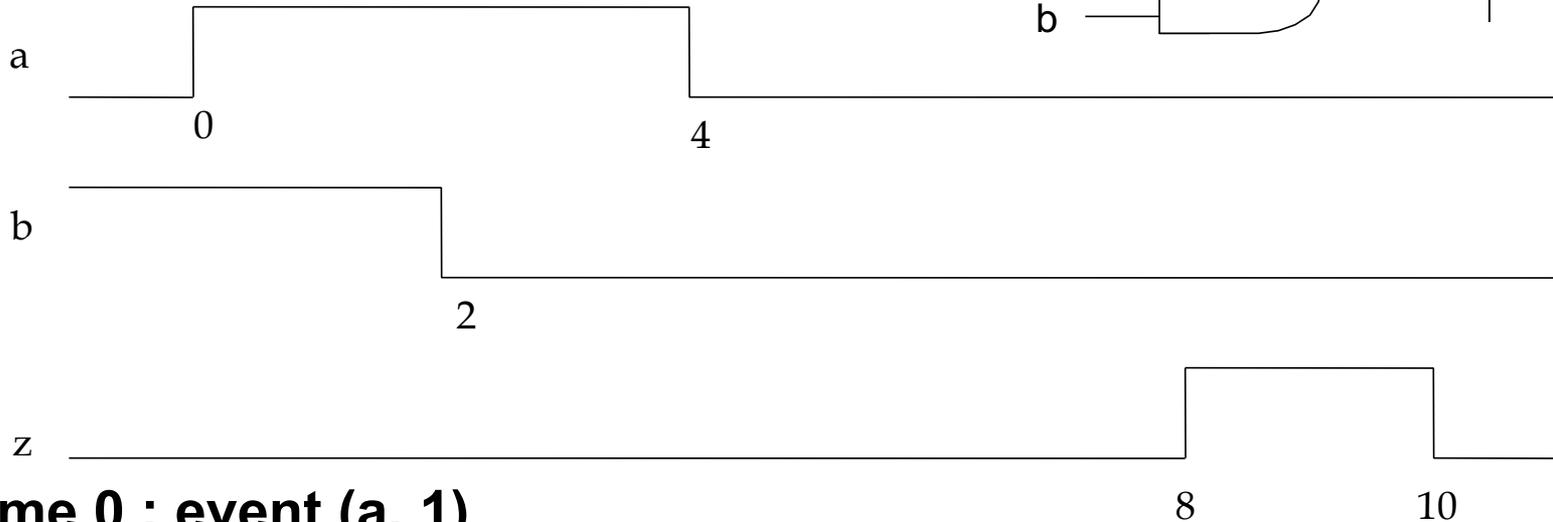
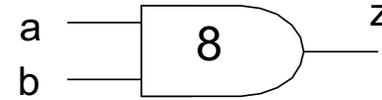
$G_3$ : 4ns

$G_4$ : 6ns

# Example (Cont.)



# Example of Algorithm 1 to schedule a Null Event



- **Time 0 : event (a, 1)**  
evaluate  $z=1 \Rightarrow (z, 1)$  scheduled for time 8
- **Time 2 : event (b, 0)**  
evaluate  $z=0 \Rightarrow (z, 0)$  scheduled for time 10
- **Time 4 : event (a, 0)**  
evaluate  $z=0 \Rightarrow (z, 0)$  scheduled for time 12

**The last scheduled event (at  $t=12$ ) is not a real event!!**

# An Improved Algorithm



Change **Pass 2** to:

```
For every $j \in \mathbf{Activated}$ {
 $v'_j = \text{evaluate}(j)$;
 if ($v'_j \neq \mathbf{lsv}(j)$) (lsv: last saved value)
 {
 schedule (j, v'_j) for time $t+d(j)$;
 $\mathbf{lsv}(j) = v'_j$;
 }
}
```

# Two Pass V.S. One Pass Algorithm



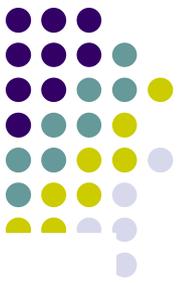
- Two-pass strategy performs the evaluations only after all the concurrent events have been retrieved
  - to avoid repeated evaluations of gates having multiple input changes.
- Experience shows, however, that most gates are evaluated as a result of only one input change.
- One-pass strategy:
  - Evaluates a gate as soon as it is activated
  - Avoids the overhead of building the Activated set

# One Pass Algorithm



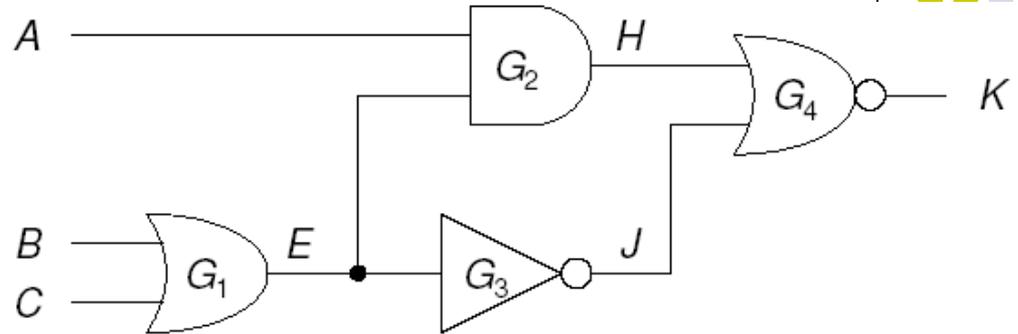
```
For every event (g, v_g^+) pending at current time t {
 $v_g = v_g^+$;
 for every j on the fanout list of g {
 update input values of j ;
 $v_j^+ = \text{evaluate}(j)$;
 if $(v_j^+ \neq v_j)$ {
 schedule (j, v_j^+) for time $t+d(j)$;
 $v_j = v_j^+$;
 }
 }
}
```

# An Example of Hazards

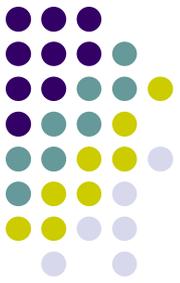


## Hazards

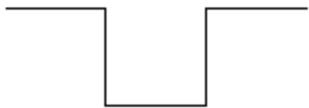
- Unwanted transient pulses or glitches



# Type of Hazards



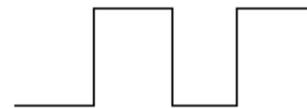
- Static or dynamic
  - A static hazard refers to the transient pulse on a signal line whose static value does not change
  - A dynamic hazard refers to the transient pulse during a 0-to-1 or 1-to-0 transition
- 1 or 0



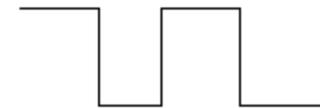
Static 1-hazard



Static 0-hazard



Dynamic 1-hazard



Dynamic 0-hazard

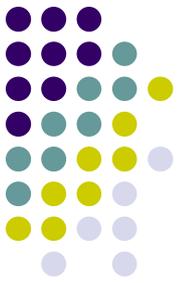
# Static Hazard Detection



- Extra encoding can be used to detect hazards during logic simulation.
  - Note that hazards only occur during signal transition
  - Two consecutive vectors are considered simultaneously
- The following is the 6-valued encoding for a pair of vectors.
  - For example, 0- $\rightarrow$ 1 transition (R) is encoded as 0X1.

| Value  | Sequence(s)     | Meaning                  |
|--------|-----------------|--------------------------|
| 0      | 000             | Static 0                 |
| 1      | 111             | Static 1                 |
| 0/1, R | {001,011} = 0x1 | Rise (0 to 1) transition |
| 1/0, F | {110,100} = 1x0 | Fall (1 to 0) transition |
| 0*     | {000,010} = 0x0 | Static 0-hazard          |
| 1*     | {111,101} = 1x1 | Static 1-hazard          |

# 6-Valued Logic for Static Hazard Analysis

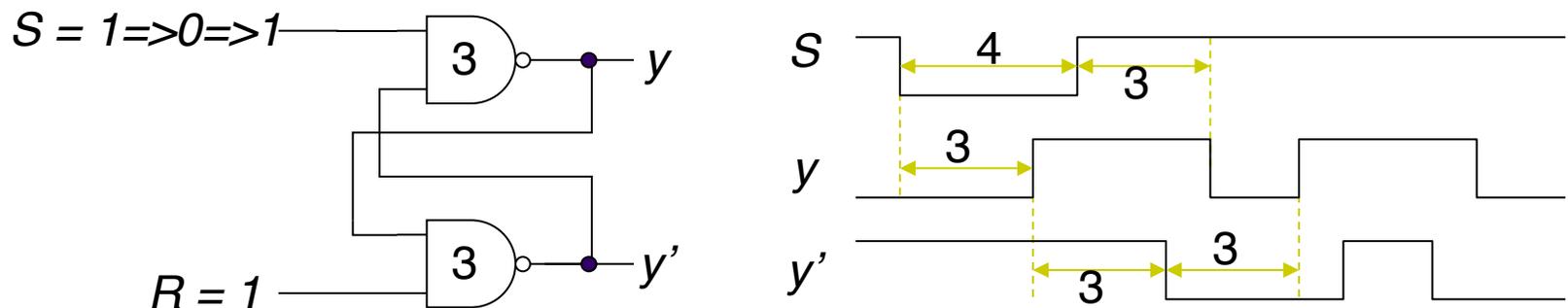


| <b>AND</b> | <b>0</b> | <b>1</b>  | <b>R</b>  | <b>F</b>  | <b>0*</b> | <b>1*</b> |
|------------|----------|-----------|-----------|-----------|-----------|-----------|
| <b>0</b>   | <b>0</b> | <b>0</b>  | <b>0</b>  | <b>0</b>  | <b>0</b>  | <b>0</b>  |
| <b>1</b>   | <b>0</b> | <b>1</b>  | <b>R</b>  | <b>F</b>  | <b>0*</b> | <b>1*</b> |
| <b>R</b>   | <b>0</b> | <b>R</b>  | <b>R</b>  | <b>0*</b> | <b>0*</b> | <b>R</b>  |
| <b>F</b>   | <b>0</b> | <b>F</b>  | <b>0*</b> | <b>F</b>  | <b>0*</b> | <b>F</b>  |
| <b>0*</b>  | <b>0</b> | <b>0*</b> | <b>0*</b> | <b>0*</b> | <b>0*</b> | <b>0*</b> |
| <b>1*</b>  | <b>0</b> | <b>1*</b> | <b>R</b>  | <b>F</b>  | <b>0*</b> | <b>1*</b> |

# Oscillation



- Oscillating circuits will result in repeated scheduling & processing of the same sequence of events

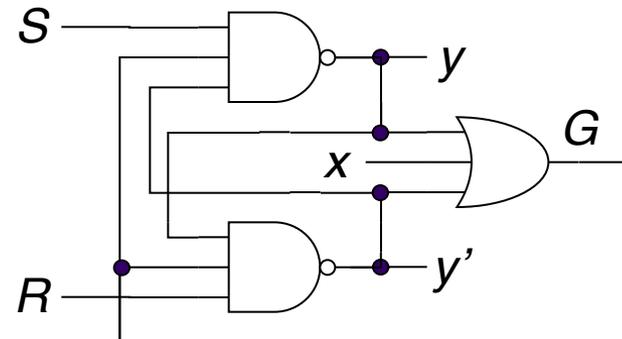
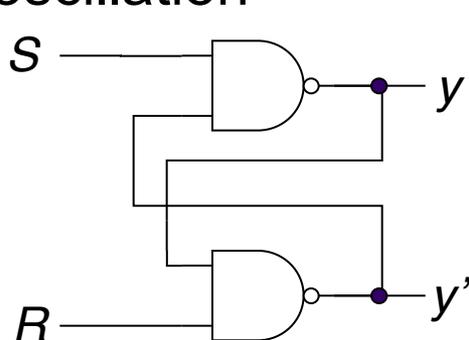


- Oscillation control takes appropriate action upon detection of oscillation

# Local Oscillation Control



- identify conditions that causes oscillations in specific sub-circuits, e.g., latches, flip-flops
  - For an oscillating latch, the appropriate corrective action is to set  $y = y' = x$  (unknown)
- Oscillation control via modeling
  - Example: when  $y=y'=0$  (oscillation condition, also implying  $S=R=1$ ),  $G = x$  causes  $y = y' = x$  and stops oscillation

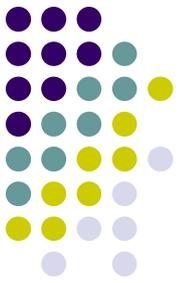


# Global Oscillation Control



- Detection of global oscillation is computationally infeasible
  - Requires detecting cyclic sequences of values for any signal in the circuit
- A typical procedure is to count the number of events occurring after any primary input change
  - Oscillation is “assumed” if the number exceeds the specified limit

# Simulation Engines



- Motivation
  - Logic simulation is time consuming.
- Simulation engines are special-purpose hardware for speeding up logic simulation.
  - Usually attached to a general-purpose host computer through, for example, VME/PCI bus.
  - FPGA-based logic emulation
- Use parallel and/or distributed processing architectures.